

Calculations Involving pH

1. What is the pH of a 1.0×10^{-4} M hydrochloric acid solution?
2. What is the pH of a 1.0×10^{-3} M sodium hydroxide solution?
3. What is the pH of a 3.5×10^{-8} M calcium hydroxide solution?
4. What is the pH of a 6.0×10^{-3} M sulfuric acid solution?
5. Determine the hydronium ion concentration of an aqueous solution that has a pH of 4.0.
6. Determine the hydronium ion concentration of an aqueous solution that has a pH of 8.0.
7. Determine the hydroxide ion concentration of an aqueous solution that has a pH of 6.2.
8. Determine the hydroxide ion concentration of an aqueous solution that has a pH of 12.5.
9. Determine the hydronium ion and hydroxide ion concentrations of an aqueous solution that has a pH of 5.1.

Calculations Involving pH

1. What is the pH of a 1.0×10^{-4} M hydrochloric acid solution?

$$= ? \text{ pH} \quad \text{HCl} + \text{H}_2\text{O} \rightarrow \text{H}_3\text{O}^+ + \text{Cl}^-$$

$$\frac{1.0 \times 10^{-4} \text{ moles HCl}}{1 \text{ L sol'n}} \left(\frac{1 \text{ mole H}_3\text{O}^+}{1 \text{ mole HCl}} \right) = 1.0 \times 10^{-4} \text{ M H}_3\text{O}^+$$

$$\text{pH} = -\log [\text{H}_3\text{O}^+] = -\log (1.0 \times 10^{-4} \text{ M}) = \boxed{4.00}$$

2. What is the pH of a 1.0×10^{-3} M sodium hydroxide solution?

$$= ? \text{ pH} \quad \text{NaOH} \xrightarrow{\text{H}_2\text{O}} \text{Na}^+ + \text{OH}^-$$

$$\frac{1.0 \times 10^{-3} \text{ mol NaOH}}{1 \text{ L sol'n}} \left(\frac{1 \text{ mole OH}^-}{1 \text{ mole NaOH}} \right) = 1.0 \times 10^{-3} \text{ M OH}^-$$

$$\text{pOH} = -\log (1.0 \times 10^{-3} \text{ M OH}^-) = 3.00$$

$$\text{pH} = 14 - 3.00 = \boxed{11.00}$$

3. What is the pH of a 3.5×10^{-8} M calcium hydroxide solution?

$$= ? \text{ pH} \quad \text{Ca(OH)}_2 \xrightarrow{\text{H}_2\text{O}} \text{Ca}^{2+} + 2 \text{OH}^-$$

$$\frac{3.5 \times 10^{-8} \text{ Ca(OH)}_2}{1 \text{ L sol'n}} \left(\frac{2 \text{ mole OH}^-}{1 \text{ mole Ca(OH)}_2} \right) = 7.0 \times 10^{-8} \text{ M OH}^-$$

$$\text{pOH} = -\log (7.0 \times 10^{-8} \text{ M OH}^-) = 7.15$$

$$\text{pH} = 14 - 7.15 = \boxed{6.85}$$

4. What is the pH of a 6.0×10^{-3} M sulfuric acid solution?

$$= ? \text{ pH} \quad \begin{aligned} \text{H}_2\text{SO}_4 + \text{H}_2\text{O} &\rightarrow \text{H}_3\text{O}^+ + \text{HSO}_4^- \\ \text{HSO}_4^- + \text{H}_2\text{O} &\rightleftharpoons \text{H}_3\text{O}^+ + \text{SO}_4^{2-} \end{aligned}$$

$$\frac{6.0 \times 10^{-3} \text{ mol H}_2\text{SO}_4}{1 \text{ L sol'n}} \left(\frac{2 \text{ mole H}_3\text{O}^+}{1 \text{ mole H}_2\text{SO}_4} \right) = 1.2 \times 10^{-2} \text{ M H}_3\text{O}^+$$

$$\text{pH} = -\log (1.2 \times 10^{-2} \text{ M H}_3\text{O}^+) = \boxed{1.92}$$

only 1 place past decimal ∴ [] has only 1 SF

5. Determine the hydronium ion concentration of an aqueous solution that has a pH of

→ $\boxed{4.0}$ $= ? [\text{H}_3\text{O}^+]$

$$\text{pH} = -\log [\text{H}_3\text{O}^+] \quad [\text{H}_3\text{O}^+] = 2^{\text{nd}} \log (-\text{pH})$$

$$[\text{H}_3\text{O}^+] = 2^{\text{nd}} \log (-4.0) = \boxed{1 \times 10^{-4} \text{ M}}$$

6. Determine the hydronium ion concentration of an aqueous solution that has a pH of

8.0. $= ? [\text{H}_3\text{O}^+]$

$$[\text{H}_3\text{O}^+] = 2^{\text{nd}} \log (-\text{pH}) \quad [\text{H}_3\text{O}^+] = 2^{\text{nd}} \log (-8.0)$$

$$= \boxed{1 \times 10^{-8} \text{ M}}$$

7. Determine the hydroxide ion concentration of an aqueous solution that has a pH of

6.2. $= ? [\text{OH}^-]$

$$\text{pH} + \text{pOH} = 14$$

$$\text{pOH} = 14 - 6.2 = 7.8$$

$$[\text{OH}^-] = 2^{\text{nd}} \log (-\text{pOH}) = 2^{\text{nd}} \log (-7.8) = \boxed{2 \times 10^{-8} \text{ M}}$$

8. Determine the hydroxide ion concentration of an aqueous solution that has a pH of 12.5. = ? $[\text{OH}^-]$

$$\begin{aligned} \text{pH} + \text{pOH} &= 14 \\ \text{pOH} &= 14 - 12.5 \\ &= 1.5 \end{aligned}$$

$$\begin{aligned} [\text{OH}^-] &= 2^{\text{nd}} \log(-1.5) \\ &= 3 \times 10^{-2} \text{ M} \end{aligned}$$

9. Determine the hydronium ion and hydroxide ion concentrations of an aqueous solution that has a pH of 5.1.

$$\begin{aligned} &= ? [\text{H}_3\text{O}^+] \\ &= ? [\text{OH}^-] \end{aligned}$$

$$\text{pH} = -\log [\text{H}_3\text{O}^+]$$

$$\begin{aligned} [\text{H}_3\text{O}^+] &= 2^{\text{nd}} \log(-\text{pH}) \\ &= 2^{\text{nd}} \log(-5.1) \\ &= 8 \times 10^{-6} \text{ M } \text{H}_3\text{O}^+ \end{aligned}$$

$$K_w = [\text{H}_3\text{O}^+][\text{OH}^-] = 1 \times 10^{-14} \text{ m}^2$$

$$\begin{aligned} [\text{OH}^-] &= \frac{K_w}{[\text{H}_3\text{O}^+]} \\ &= \frac{1 \times 10^{-14} \text{ m}^2}{8 \times 10^{-6} \text{ m}} \end{aligned}$$

$$= 1. \times 10^{-9} \text{ m } [\text{OH}^-]$$